

# EEC4122: Satellite Communication Systems (Fall 2015)

## Chapter 3: The Geostationary Orbit

### Problem Set

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November 2, 2015

**P1:** (a) Explain why there is only one geostationary orbit.

(b) Show that the range  $d$  from an earth station to a geostationary satellite is given by

$$d = \sqrt{(R \sin El)^2 + h(2R + h)} - R \sin El,$$

where  $R$  is the earth radius (assumed spherical),  $h$  is the height of the geostationary orbit above the equator, and  $El$  is the elevation angle of the earth station antenna.

**P2:** Determine the latitude and longitude of the farthest north earth station which can link with any given geostationary satellite. The longitude should be given relative to the satellite longitude, and a minimum elevation angle of  $5^\circ$  should be assumed for the earth station antenna. A spherical earth of mean radius 6371 km may be assumed.

**P3:** An earth station is located at latitude  $35^\circ\text{N}$  and longitude  $100^\circ\text{W}$ . Calculate the antenna-look angles for a satellite at  $67^\circ\text{W}$ .

**P4:** Calculate for your home location the look angles required to receive from the satellite

(a) immediately east and (b) immediately west of your longitude.

**P5:** An earth station at latitude  $30^{\circ}\text{S}$  is in communication with an earth station on the same longitude at  $30^{\circ}\text{N}$ , through a geostationary satellite. The satellite longitude is  $20^{\circ}$  east of the earth stations. Calculate the antenna-look angles for each earth station and the round-trip time, assuming this consists of propagation delay only.

**P6:** Determine the maximum possible longitudinal separation which can exist between a geostationary satellite and an earth station while maintaining line-of-sight communications, assuming the minimum angle of elevation of the earth station antenna is  $5^{\circ}$ . State also the latitude of the earth station.

**P7:** Calculate the angle of tilt required for a polar mount antenna used at your home location.

**P8:** The borders of a certain country can be roughly represented by a triangle with coordinates  $39^{\circ}\text{E}, 33.5^{\circ}\text{N}$ ;  $43.5^{\circ}\text{E}, 37.5^{\circ}\text{N}$ ;  $48.5^{\circ}\text{E}, 30^{\circ}\text{N}$ . If a geostationary satellite has to be visible from any point in the country, determine the limits of visibility (i.e., the limiting longitudinal positions for a satellite on the geostationary arc). Assume a minimum angle of elevation for the earth station antenna of  $5^{\circ}$ , and show which geographic location fixes which limit.